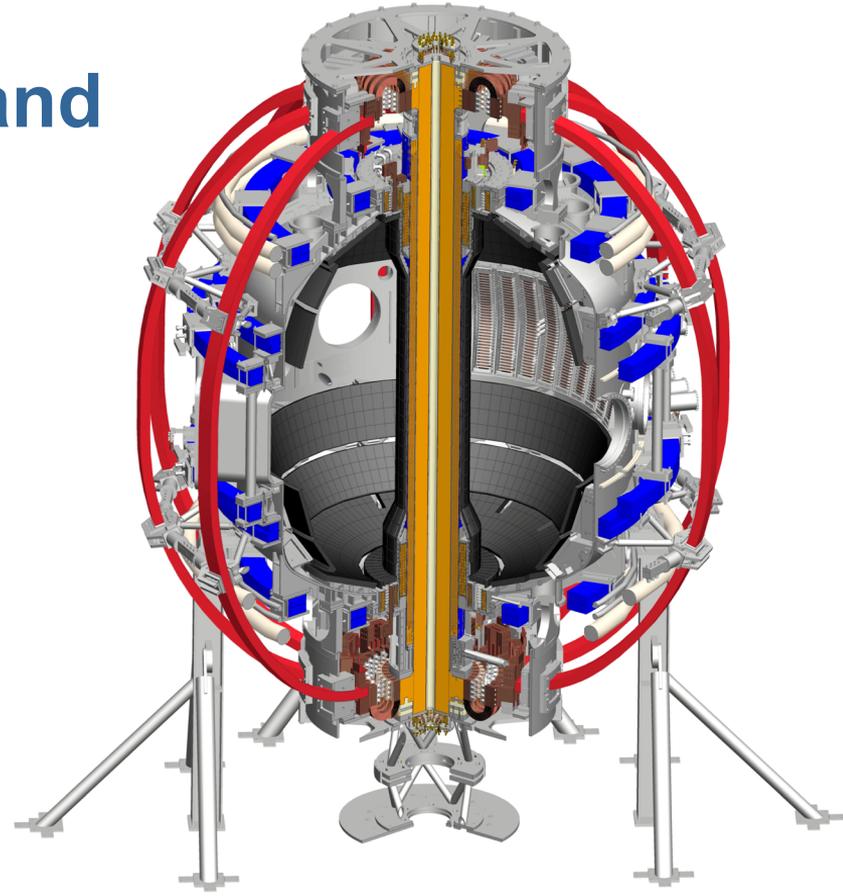


# Introduction to Tokamaks and Spherical Tokamaks

2020 SULI Introduction to Fusion Energy  
and Plasma Physics Course

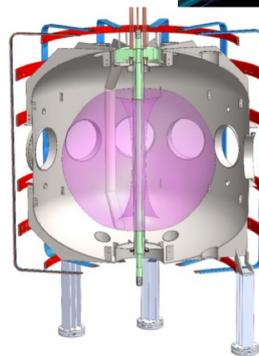
Devon Battaglia

June 18, 2020



# Who am I?

- Introduced to fusion energy research in a high school summer program at the Laboratory for Laser Energetics (University of Rochester)
  - I became enamored with the atmosphere within the Control Room of a big, collaborative experiment
  - Construction of a fusion reactor is a grand project that could be a “giant leap” toward a sustainable future for humans on Earth
- B.S. Engineering Physics, B.A. in Music at Lehigh University
  - Five year Arts-Engineering program
- PhD in Nuclear Engineering – Engineering Physics (NEEP) University of Wisconsin - Madison
  - Thesis research on Pegasus, a spherical tokamak experiment
- Post-doctorial appointments at US tokamaks: NSTX and DIII-D
- Research Scientist and Lead Physics Operator at NSTX-U
  - I am living my “Gene Krantz” dream

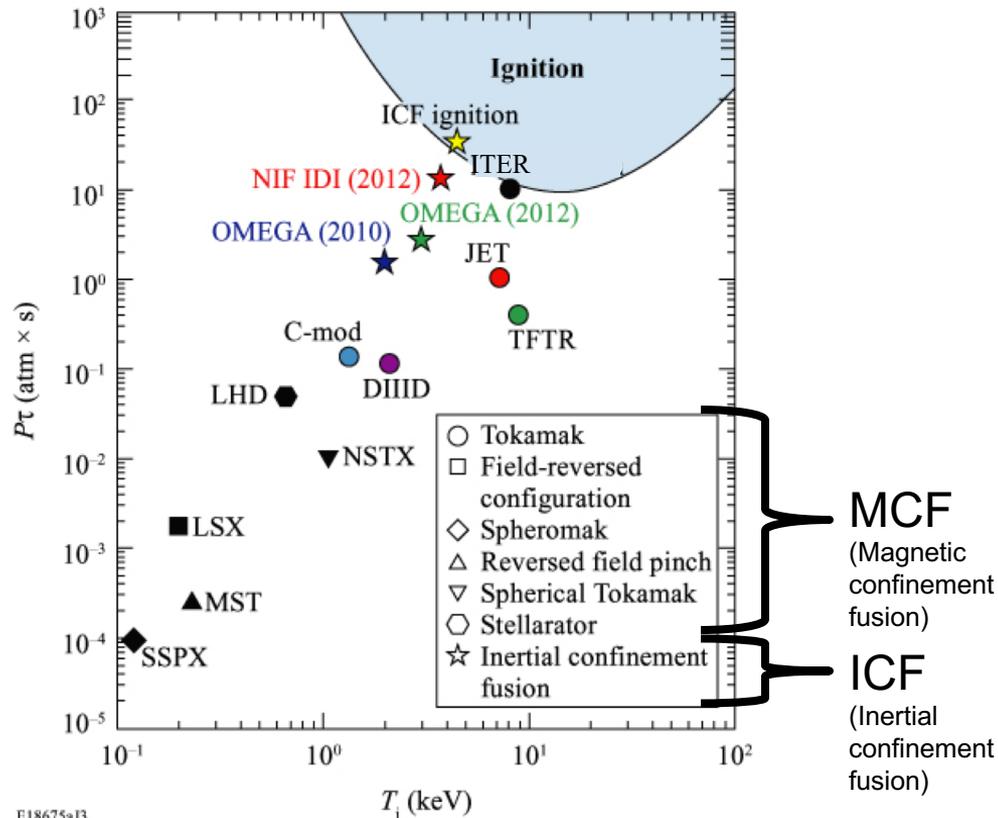


Gene Krantz, NASA NSTX-U Control room



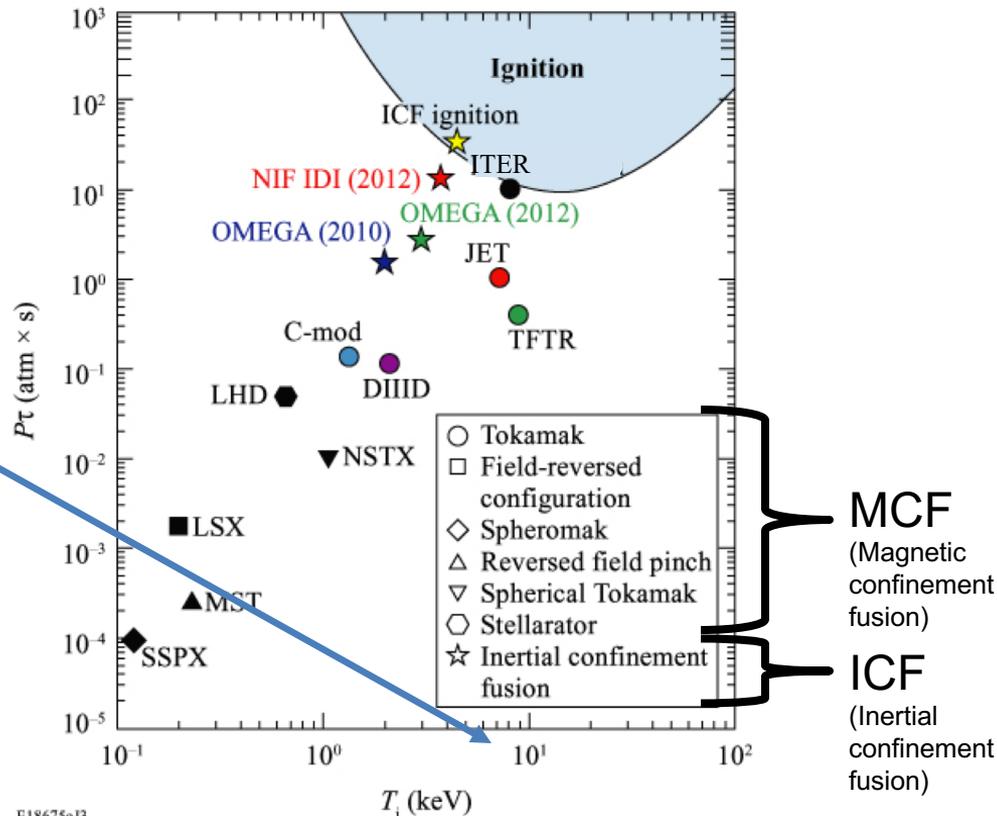
# Fusion experiments are approaching ignition conditions

- Ignition: fusion reactions completely sustain plasma temperature



# Fusion experiments are approaching ignition conditions

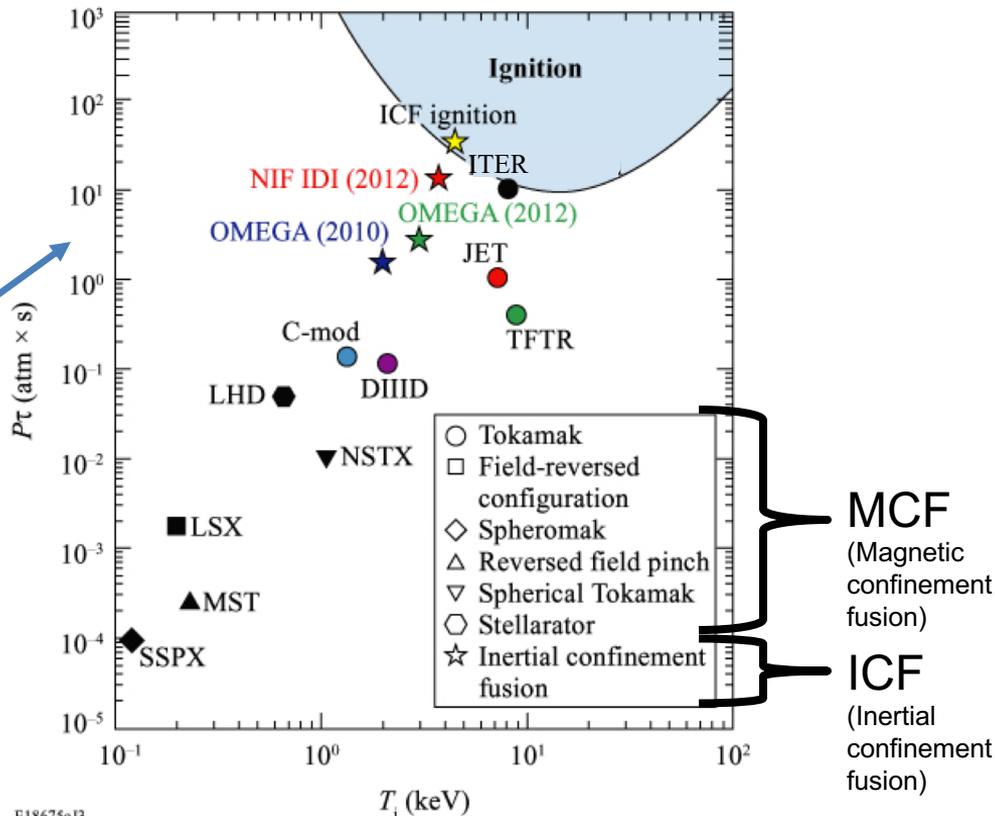
- Ignition: fusion reactions completely sustain plasma temperature
- Plasma temperature  $\sim 10$  keV
  - Dictated by fusion cross-section of deuterium-tritium



E18675aJ3

# Fusion experiments are approaching ignition conditions

- Ignition: fusion reactions completely sustain plasma temperature
- Plasma temperature  $\sim 10$  keV
  - Dictated by fusion cross-section of deuterium-tritium
- Must achieve critical  $p\tau$ 
  - Pressure = density x temperature
    - Increase pressure with density
  - Energy confinement time ( $\tau$ ) is the exponential decay time constant of the stored energy
    - Larger  $\tau \rightarrow$  energy leaks slower

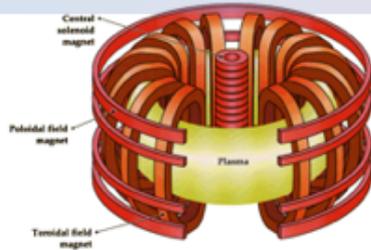


E18675aJ3

# There are many ways to make a “star in a jar”

Continuous

Magnetic Confinement (MCF)



Hold on to a super hot plasma for hours, days, weeks ...

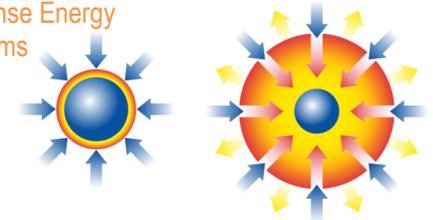
**Density:**  $10^{20} \text{ m}^{-3}$

**Confinement time ( $\tau$ ):** seconds

Magnetized target fusion (MTF)

Pulsed  
Inertial Confinement (ICF)

Intense Energy  
Beams



Implode many new fuel pellets every second

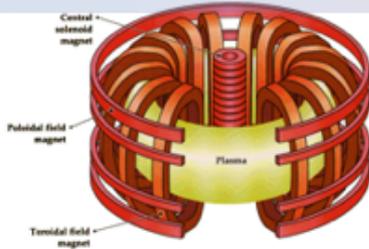
**Density:**  $10^{31} \text{ m}^{-3}$  ( $10^3 \times$  solid)

**Confinement time ( $\tau$ ):**  $10^{-10}$  seconds

# There are many ways to make a “star in a jar”

Continuous

Magnetic Confinement (MCF)



Hold on to a super hot plasma for hours, days, weeks ...

Tokamaks

Stellarators

Day 4 Bader

Reversed-field pinch

Spheromaks

Field-reversed configurations

...

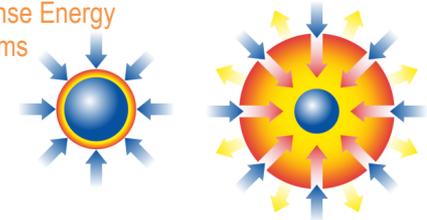
Magnetized target fusion (MTF)

Day 5  
Sefkow

Pulsed

Inertial Confinement (ICF)

Intense Energy  
Beams



Implode many new fuel pellets every second

Day 10  
Ma

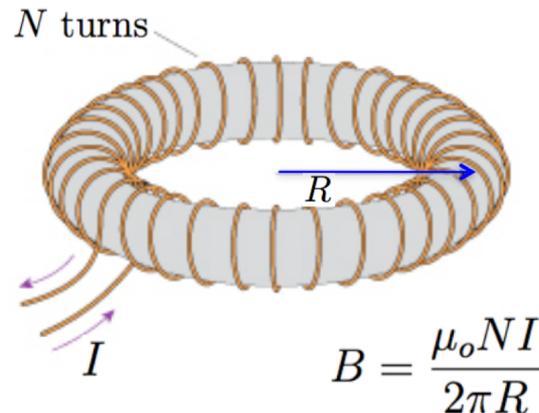
# Outline

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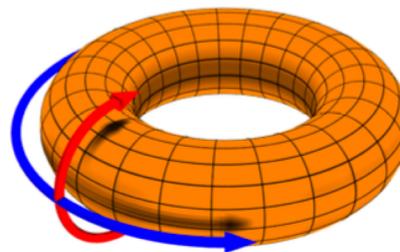
- Introduction to tokamaks
- Tokamak design considerations
- Present-day tokamak research

# Flashback to Tuesday

- What if we make a magnetic bottle that looks like a donut?
  - With only a toroidal field, the charged particles drift outward
- Solution: twist the magnetic field by adding a poloidal magnetic field
  - Creates magnetic surfaces



**Toroidal direction**  
**Poloidal direction**

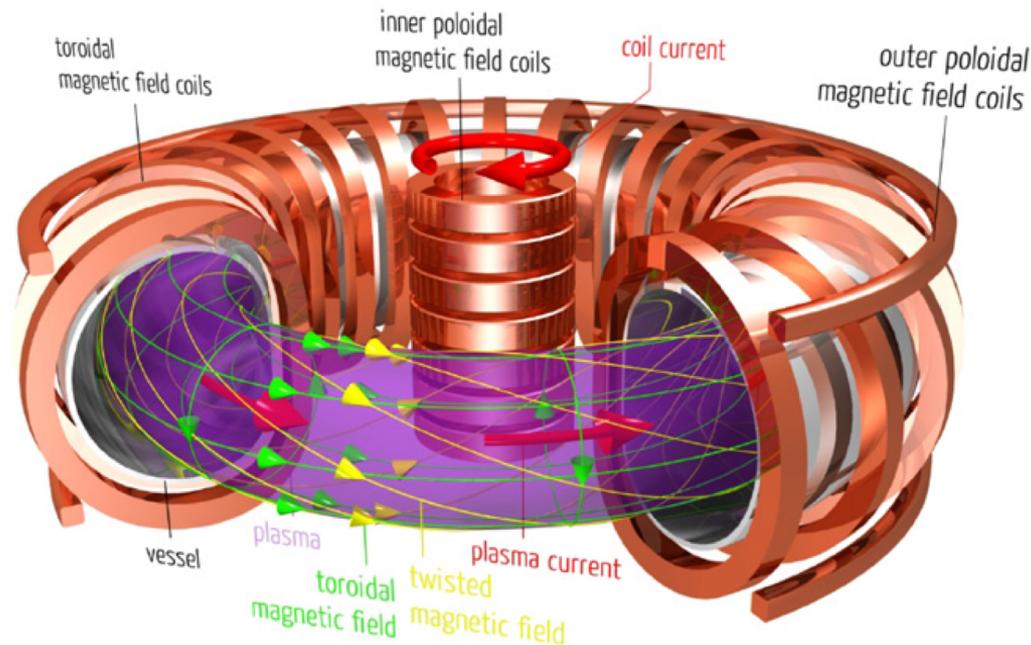


Day 2  
Fox

# Two leading schemes for making helical magnetic fields to confine a hot plasma for seconds, minutes, days ...

## 1) Tokamak

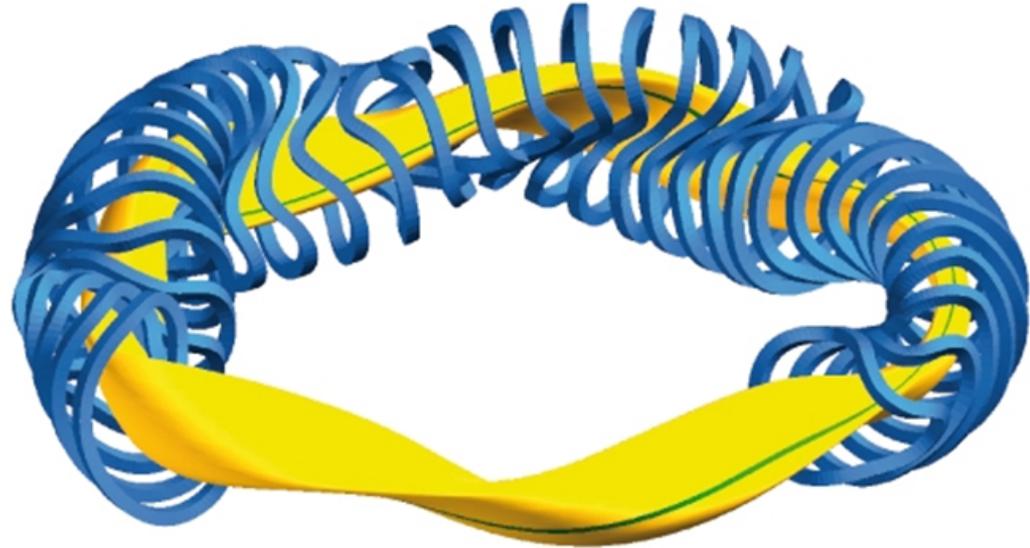
- External coils produce toroidal field
- Drive a toroidal current through the plasma ( $I_p$ ) to produce a poloidal field
- Demonstrated largest  $\rho\tau$  of all MCF concepts



# Two leading schemes for making helical magnetic fields to confine a hot plasma for seconds, minutes, days ...

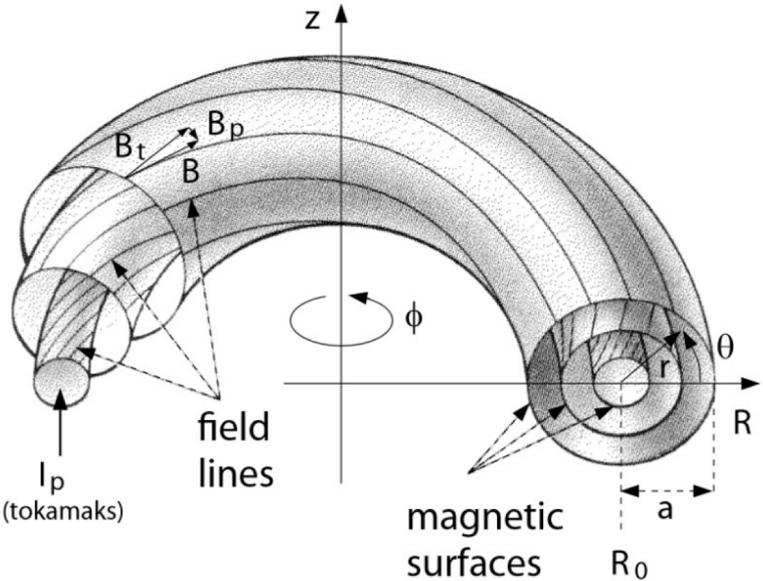
## 2) Stellarator

- External coils produce twisted magnetic field
- Easier to operate for long periods of time since no plasma current is needed
- Recent innovations have enabled the design and construction of optimized stellarators



Day 4 Bader

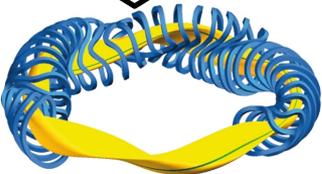
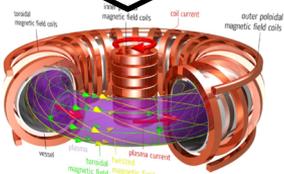
# Each magnetic surface has field lines of a given helicity



$q = 2\pi/l_i = \text{toroidal transits} / \text{poloidal transit}$

“q” !!  
Safety factor!!

“iota” !!  
Rotational transform!!



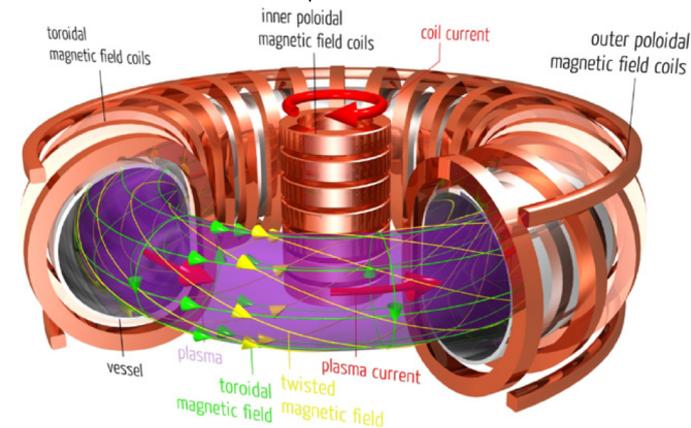
Let's call the whole thing off ...

Convenient to reduce 3D toroidal coordinates  $(\phi, \theta, R)$  to 1D magnetic surface coordinates  $(\psi)$  when possible

# Toroidal current must be sustained in a tokamak

- Induce current using a central solenoid
  - Cannot sustain current indefinitely
  - Could be used to start up the plasma current
- Tokamaks have a self-driven *bootstrap current*
  - Accounts for about  $60\% \pm 20\%$  of the needed current
- Must sustain current using external sources
  - Described in next slide
- Rapid loss of plasma current leads to the rapid loss of the plasma confinement
  - This is called a *disruption*
  - Really important to avoid in a reactor
  - Stellarators do not have this issue (we think)

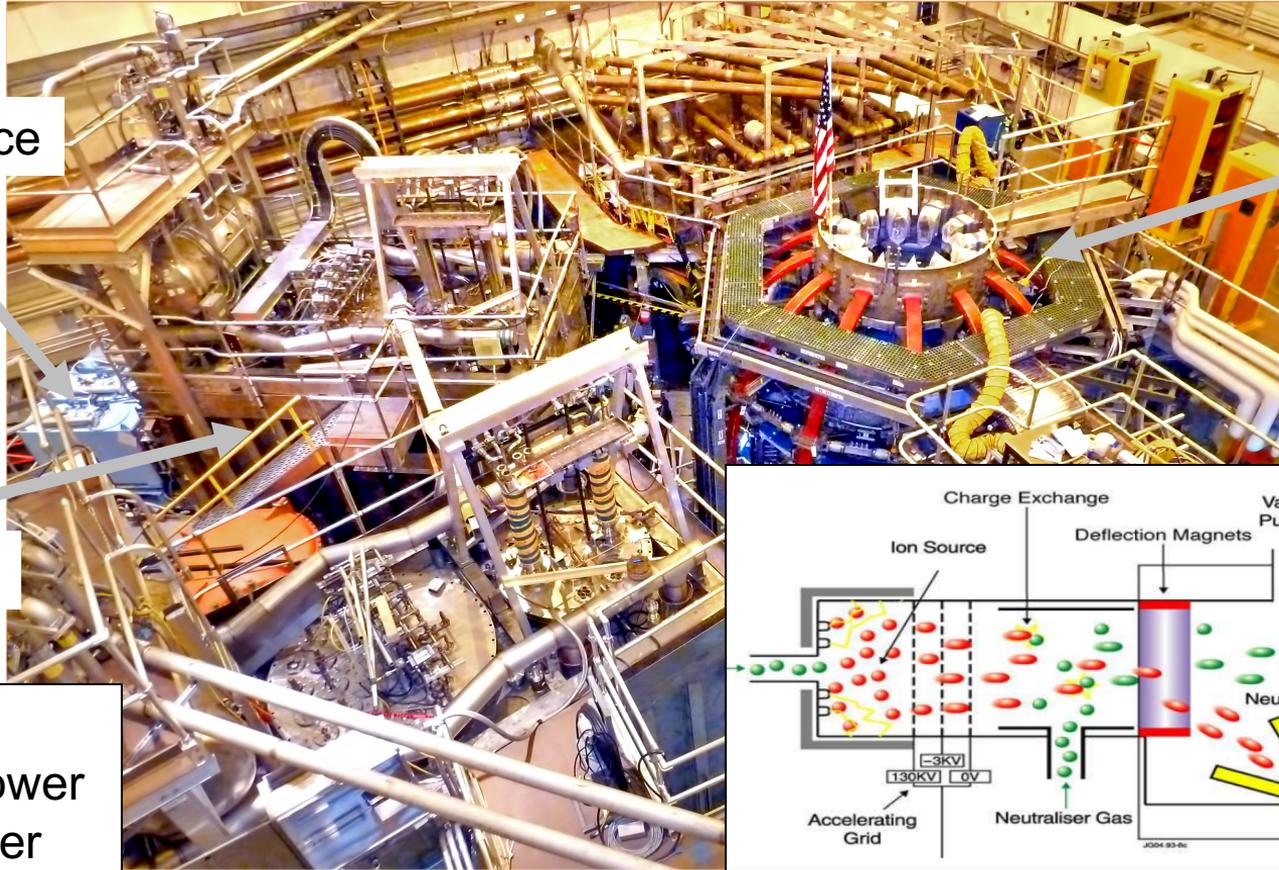
$$I_p \propto V_\phi = -\frac{d\Phi_{CS}}{dt} \propto \frac{dI_{CS}}{dt}$$



# Radio Frequency (RF) and Neutral Beam Injection (NBI) are the primary methods for current drive on tokamaks

- RF and NBI can heat the plasma and drive current
  - Tokamak reactors need efficient current drive
  - RF will be discussed tomorrow Day 5 Pinsker
- NBI: powerful beams of neutral particles
  - Neutral particles can cross the magnetic fields
  - Once inside the plasma, fast neutral particles may lose their electron to become a fast ion trapped in the magnetic field
  - Fast ions collide with colder ions and raise the plasma temperature
  - Will also fuel the plasma, drive current and induce plasma rotation
- Other current drive methods may be possible
  - Helicity injection will be discussed later today Day 4 Sutherland

# NBI systems can be as big as the tokamak

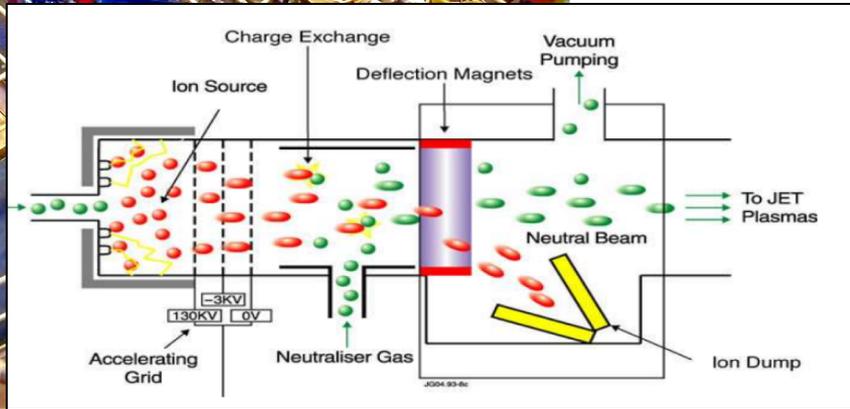


NBI ion source

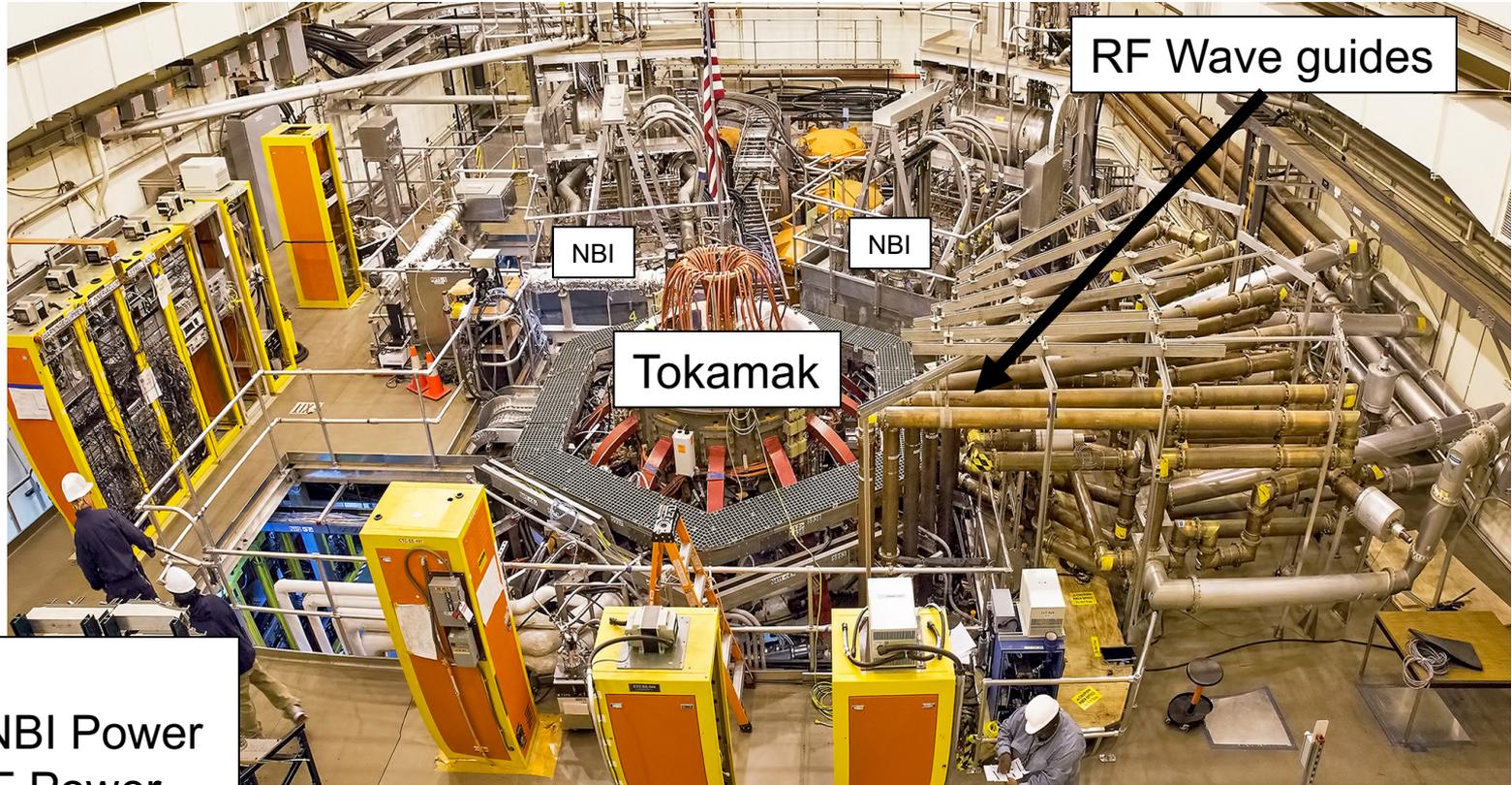
Tokamak

NBI beam box

NSTX-U  
12 MW NBI Power  
6 MW RF Power



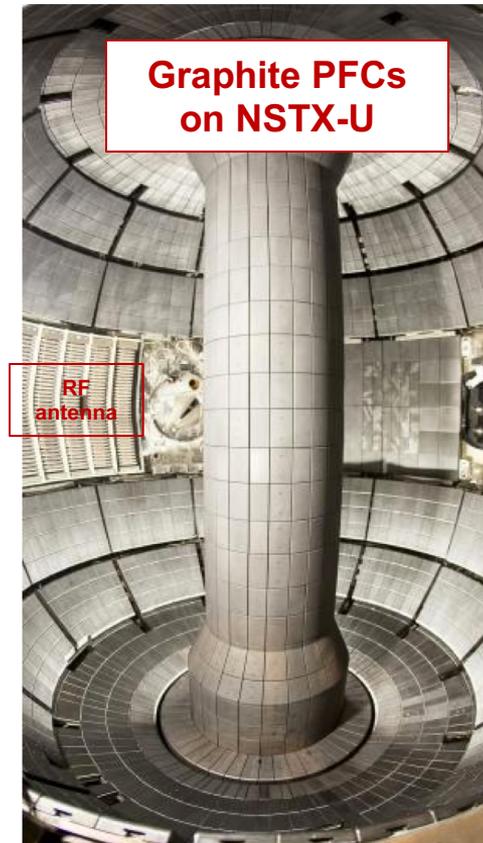
# RF sources can be far away from the tokamak and connected to an antenna using wave guides



NSTX-U  
12 MW NBI Power  
6 MW RF Power

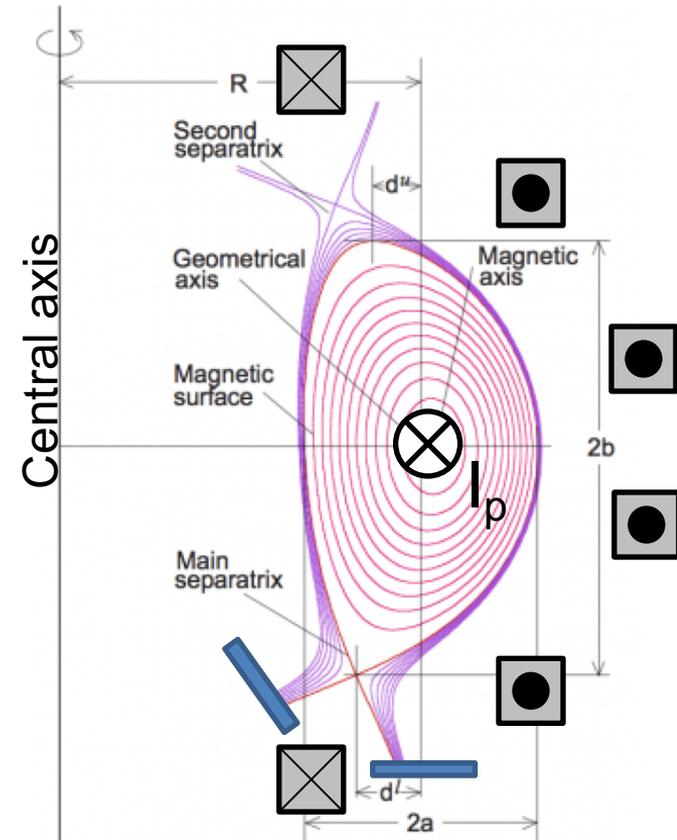
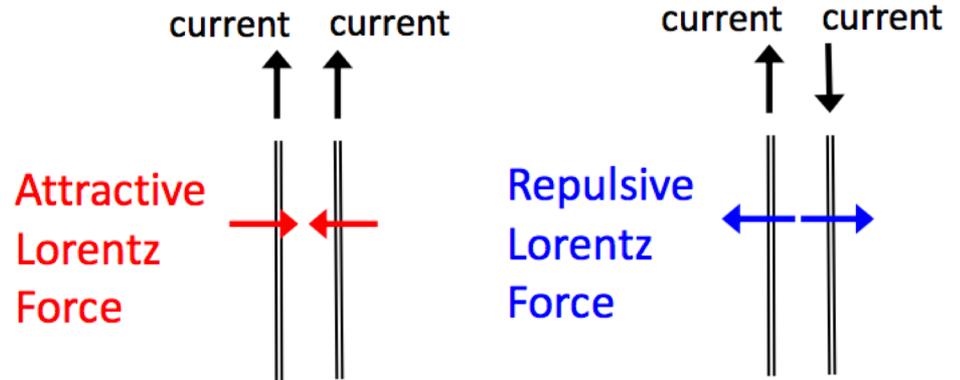
# It is best to keep the hot plasma from touching the wall of the container

- Plasmas are created in a vacuum vessel
  - Vessel is pumped down to ultra-high vacuum
- Anything in the plasma that is not deuterium or tritium is an impurity
  - Impurities dilute the fuel and can bleed away energy from the plasma via radiation
- The plasma facing components (PFCs) are a source of impurities into the plasma
  - Best to "levitate" the plasma inside the vessel to avoid direct contact



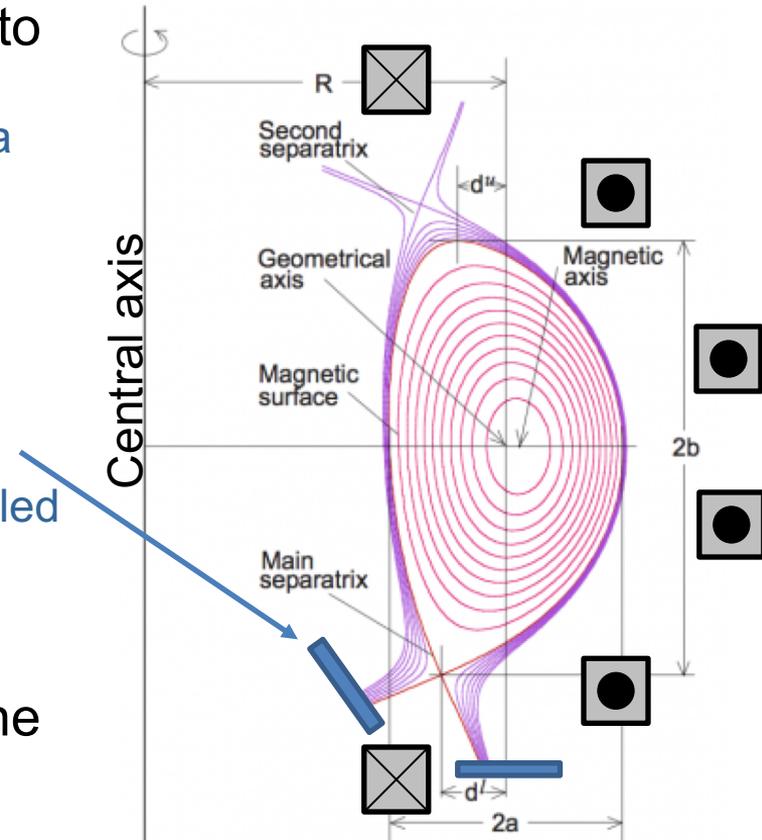
# External poloidal magnetic fields shape the plasma

- Plasma wants to expand like a tire tube due to pressure and toroidal current
  - Use external poloidal magnetic fields to maintain a stable (i.e. equilibrium) position inside the vessel



# External poloidal magnetic fields shape the plasma

- Plasma wants to expand like a tire tube due to pressure and toroidal current
  - Use external poloidal magnetic fields to maintain a stable (i.e. equilibrium) position inside the vessel
- Coils with current in the same direction as  $I_p$  will create magnetic X-points
  - Produces a *scrape-off layer (SOL)* with *open* field lines that intersect divertor plates
  - Last magnetic surface with *closed* field lines is called the *separatrix*
- It is good to socially distance where most impurities are created (divertor plates) and the edge of the confined plasma (separatrix)



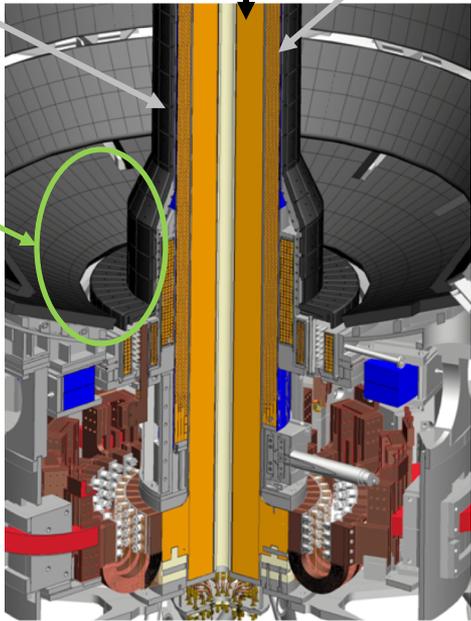
# NSTX-U: National Spherical Torus Experiment

Plasma facing components

Inner TF legs

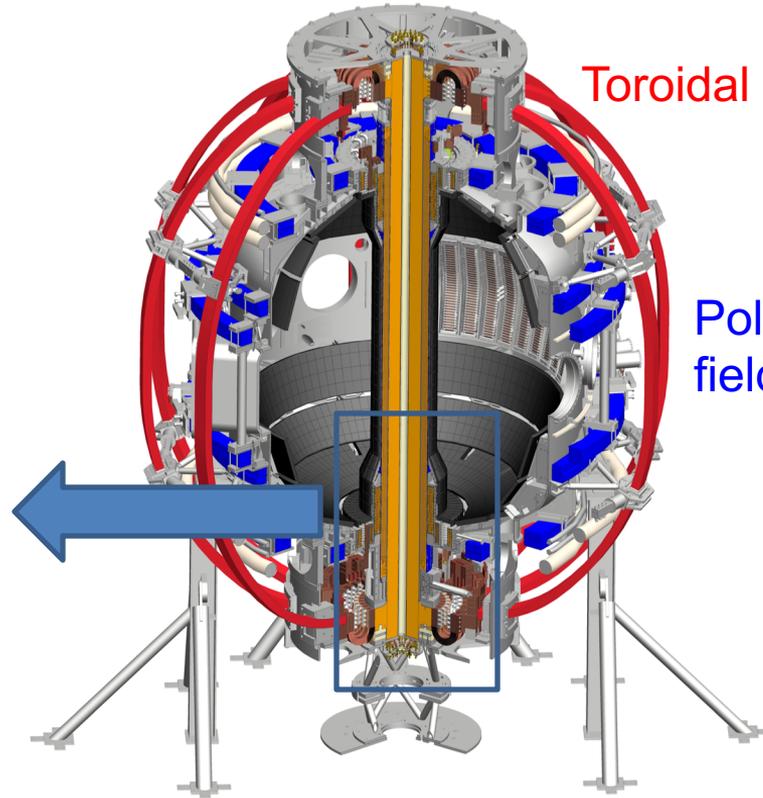
Solenoid

Divertor plates



Toroidal field coils

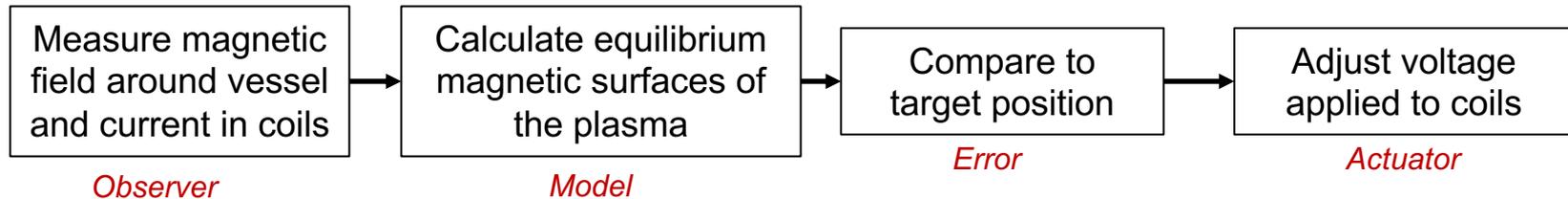
Poloidal field coils



# Real-time feedback is used to maintain the plasma position inside the vessel

- Movie of plasma discharge on the MAST experiment:  
<https://www.youtube.com/watch?v=Yu9C5TEhAdQ>

## Example of real-time (sub-millisecond) control scheme



## One of the many cool things about working in this field:

Scientists and engineers come from all sorts of backgrounds to contribute to the realization of fusion energy. Real-time control of non-linear, multi-scale systems is a research field in and of itself and fusion energy is just one application.

# Outline

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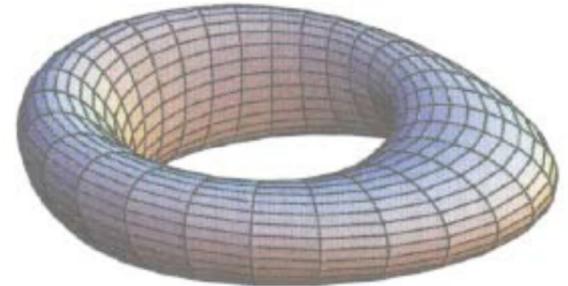
- Introduction to tokamaks
- Tokamak design considerations
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# There is a limit to $I_p$ in a tokamak

- Energy confinement ( $\tau$ ) improves with larger  $I_p$ 
  - As  $I_p$  increases, the magnetic field lines make fewer toroidal transits for each poloidal transit

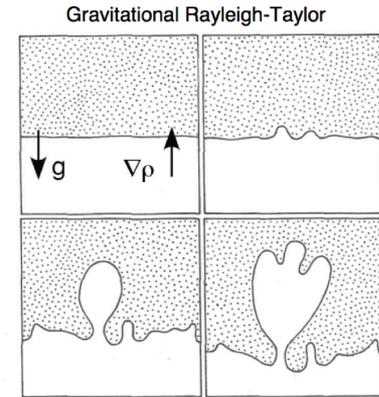
$$q_* = \frac{2\pi}{\mu_0} \frac{B_\phi}{I_P} \frac{a^2}{R}$$

- If  $q$  is too small, the magnetic field can kink
  - Thus  $q$  is the “safety factor”



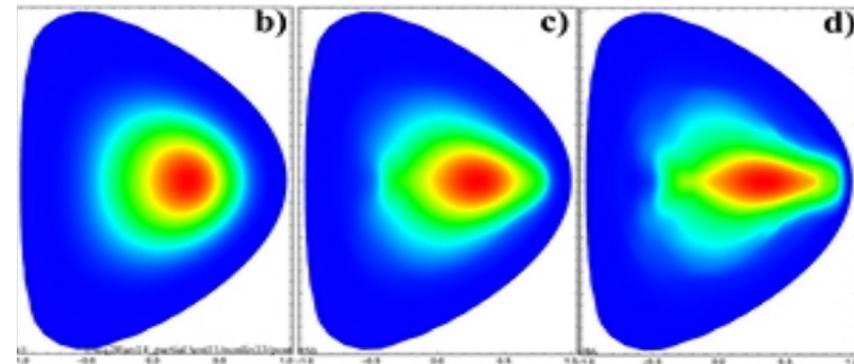
# There is a limit to the achievable plasma pressure for all magnetic confinement schemes

- An (imperfect) analogy: restoring force of the magnetic field is gravity in the familiar Rayleigh-Taylor instability
  - Plasma can *balloon* and degrade confinement ( $\tau$ )
- Pressure limits are expressed in terms of a normalized pressure called beta:

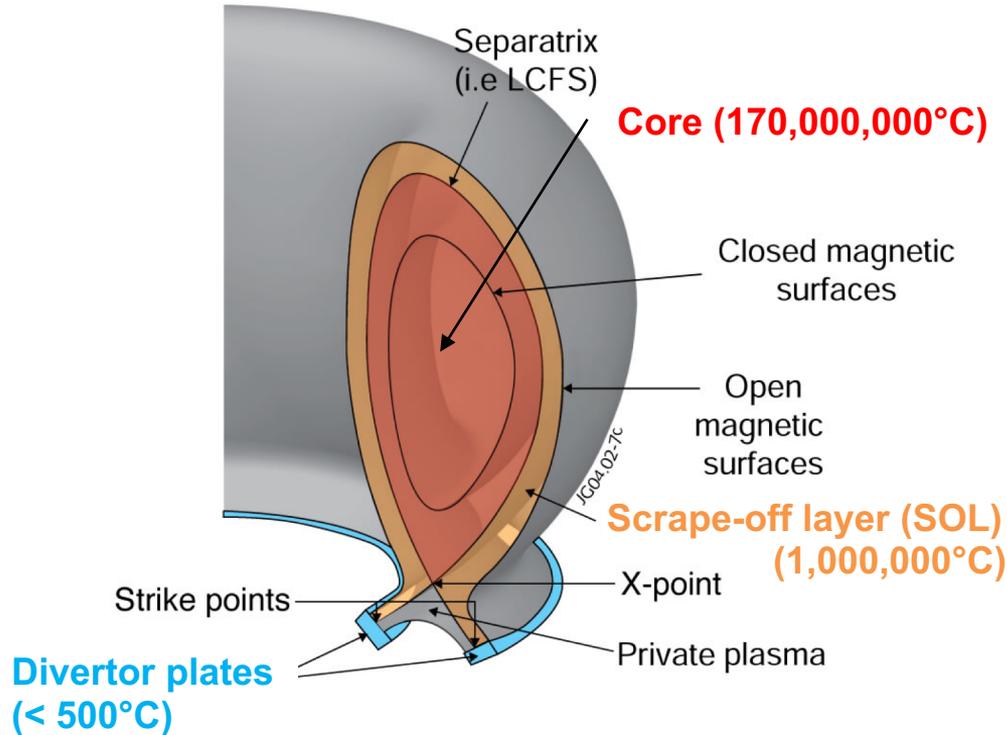


$$\beta = \frac{\text{plasma pressure}}{\text{magnetic pressure}}$$

$$\beta = \frac{2\mu_0 \langle p \rangle}{B^2}$$



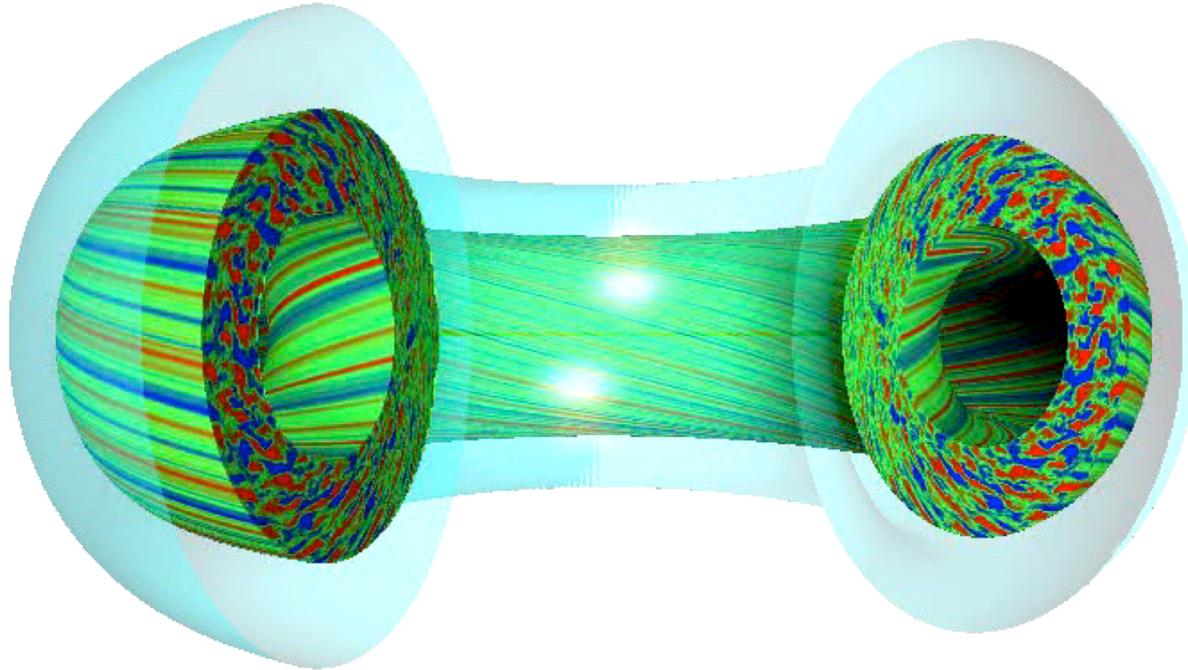
# Insulating the hot core from the “cold” wall impacts the size of the reactor



- Core temperature dictated by ideal temp for D-T fusion
- Physical distance between core and separatrix related to the achievable temperature gradient ( $\nabla T$ )
  - Larger  $\nabla T \rightarrow$  more compact
- Energy confinement time ( $\tau$ ) describes how energy diffuses (leaks) across the gradient
  - Larger  $\tau \rightarrow$  slower leak

Day 1  
Cowley

# Plasma turbulence is typically what leaks the most energy from the core



Day 2  
Mordijck

Calculations enabled by recent advances in supercomputing

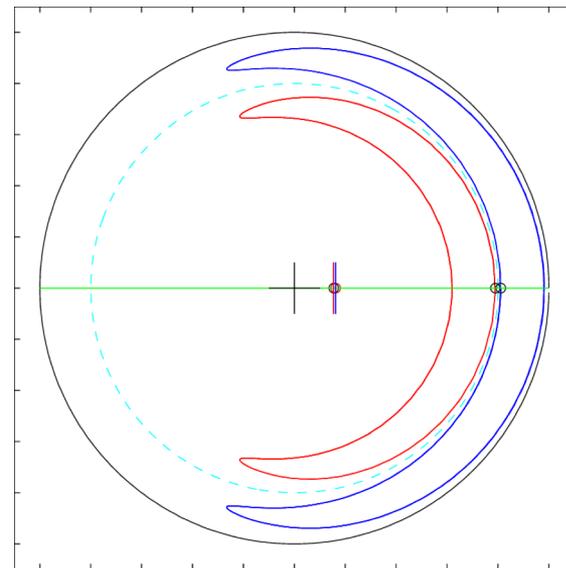


# Energy also leaks from the plasma by radiation and conduction (collisions)

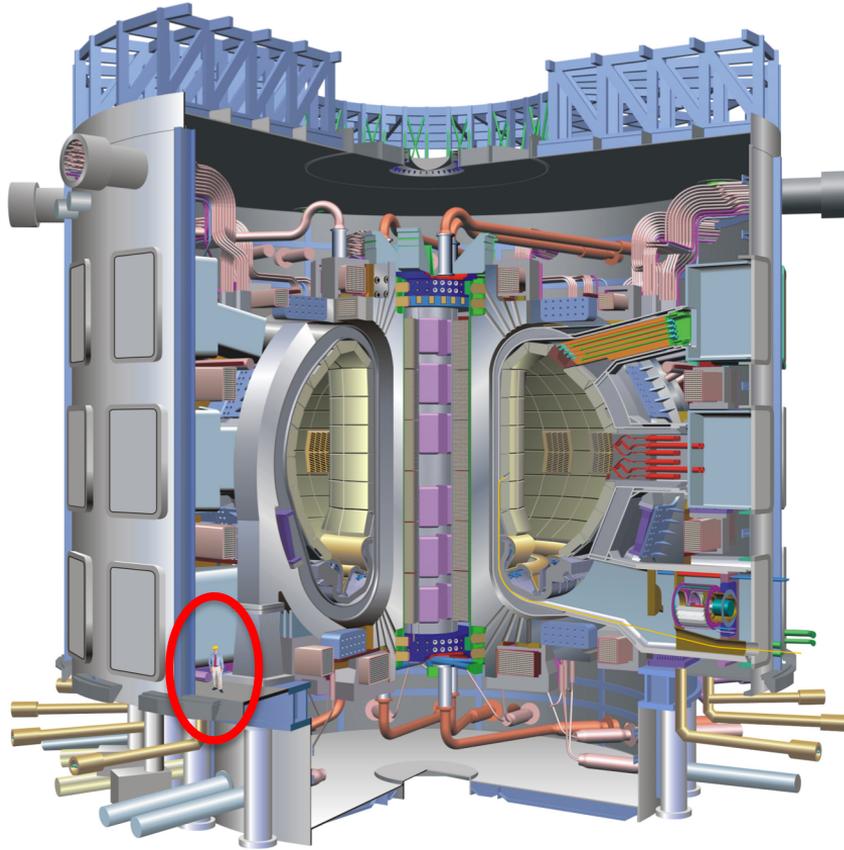
- Just like the sun, laboratory plasmas emit radiation across the electromagnetic spectrum
  - Really useful for diagnosing the plasma
- In toroidal systems, collisions between particles on *banana* orbits set the energy diffusion step size
  - Mathematics describing diffusion in a toroidal system is called *neo-classical theory*
  - Existence of banana orbits leads to the bootstrap current

Day 5  
Reinke

Day 2 Fox



# Present magnet technology and tokamak physics understanding leads to big fusion reactors



- ITER designed to produce a DT plasma with fusion energy ten times greater than the heating energy
  - Majority of plasma heating comes from fusion reactions
  - Will not put energy on the grid
- It is a grand engineering and science challenge
  - EU, Japan, US, China, Russia, South Korea and India all contributing

Day 4  
Laggner

# Outline

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- Introduction to tokamaks
- Tokamak design considerations
- Present-day tokamak research

# After ITER, what comes next?

- One option is to take technology proven on ITER to build the first demonstration fusion reactor (pilot plant)
  - Building an “ITER-like” pilot plant will require a lot of capital
  - Studies suggest this design choice can be economically competitive in markets with a cap placed on carbon emissions
- World-wide magnetic confinement fusion research is focused on two main goals:
  - Make the first study of burning plasmas in ITER a success
  - Develop innovations that reduce the capital needed to construct a pilot plant and make it attractive for the energy sector

Day 1  
Umstätt

# US tokamak research community is pursuing compact fusion reactors

- Compact tokamak concepts could reduce the capital cost of a fusion energy reactor

Day 7  
Guttenfelder

- Requires innovations in

- Magnetic field coils
- First wall materials
- Construction and maintenance
- Heating and current drive
- Blanket design and tritium breeding

Day 5 Sorbom

Day 6 Donovan,  
Lasa, Allain

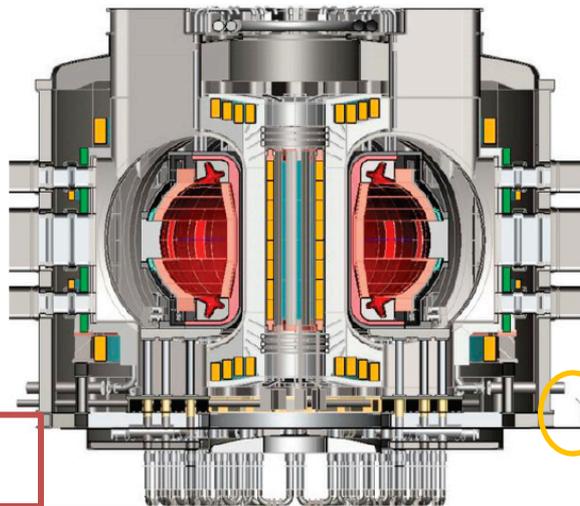
Day 7 Humrickhouse,  
Garrison

Day 5 Pinsker

Day 6 Kessel  
Day 7 Xiao

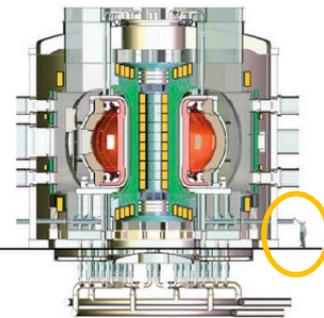
K-DEMO 6.8-m device

$P_{elec} \sim 200-600 \text{ MW}$ ,  $TBR > 1$   
 $\langle W_n \rangle > 2.09 \text{ MW/m}^2$



PPPL 4.0-m  
AT Pilot Plant

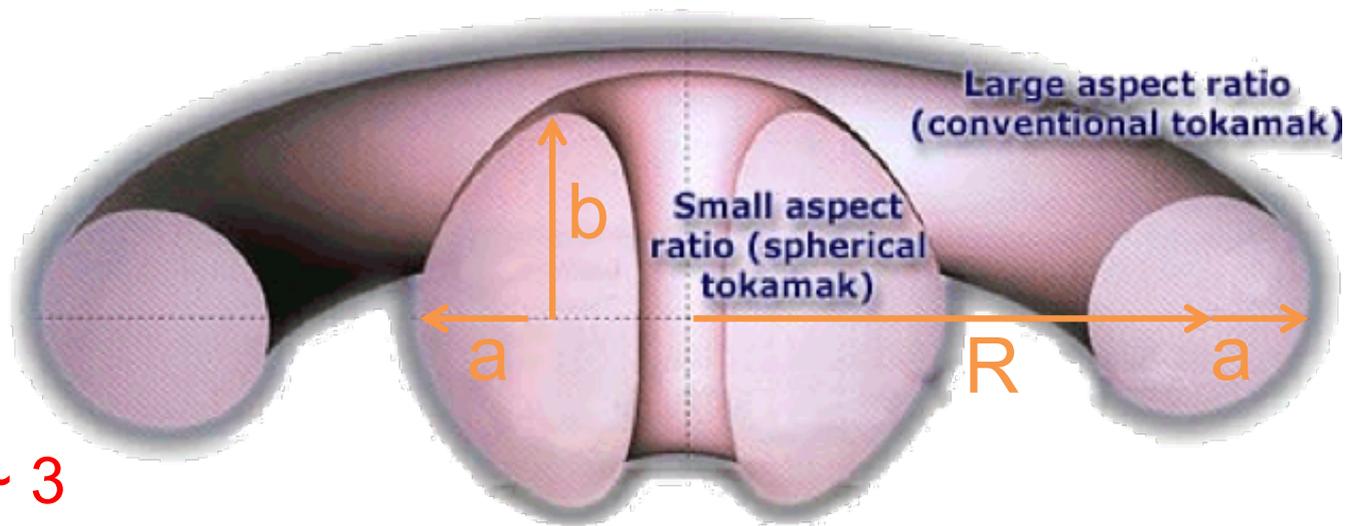
$Q_{enr} \geq 1$ ,  $TBR > 1$   
 $\langle W_n \rangle > 1.7-2.2 \text{ MW/m}^2$



# Aspect ratio and elongation are free parameters in the design of a tokamak

Aspect ratio  $A = R / a$ , Elongation  $\kappa = b / a$

$R$  = major radius,  $a$  = minor radius,  $b$  = vertical  $\frac{1}{2}$  height



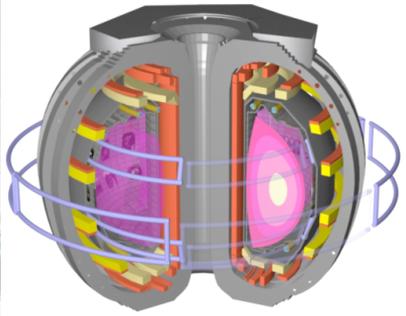
$$A \sim 3$$

$$\kappa = 1.5 - 2$$

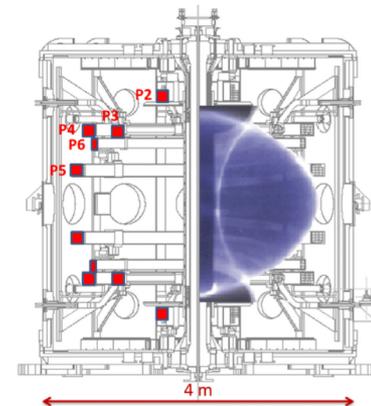
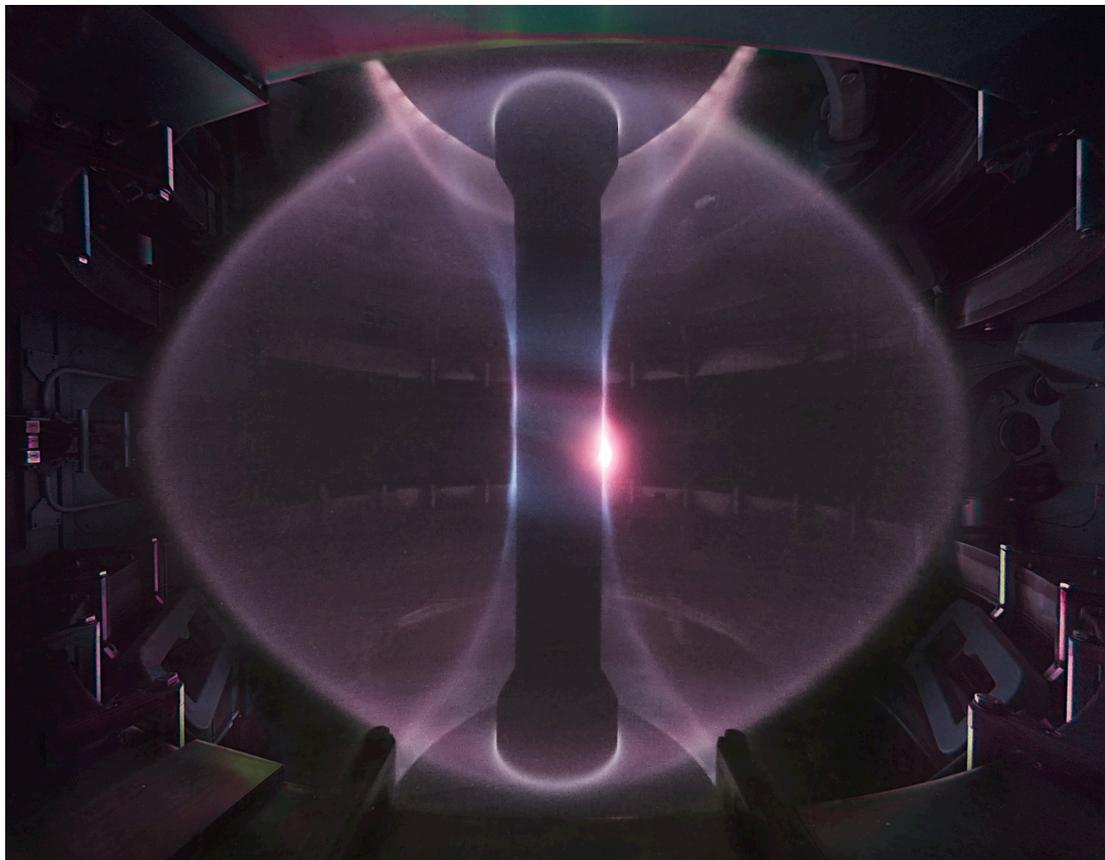
$$A \sim 1.5$$

$$\kappa = 2 - 3$$

# Inside the DIII-D tokamak: it looks like a donut



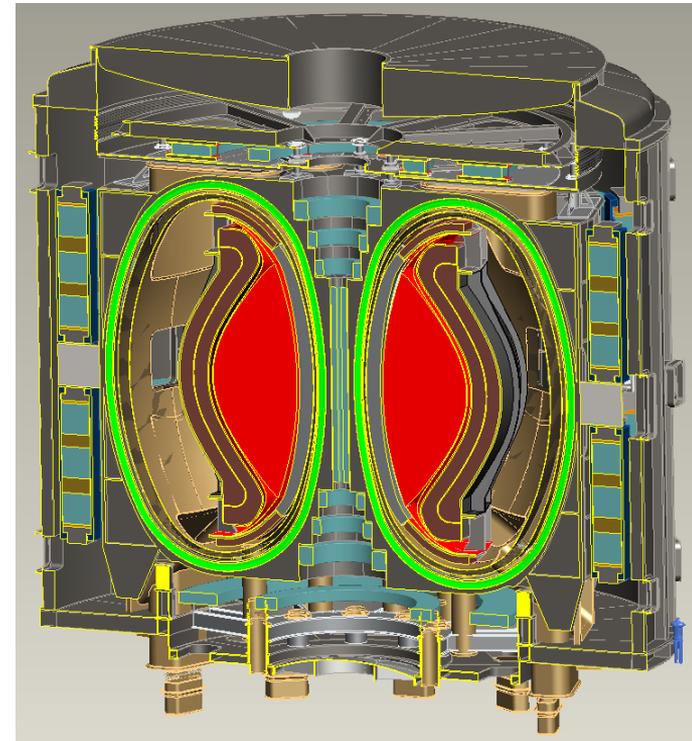
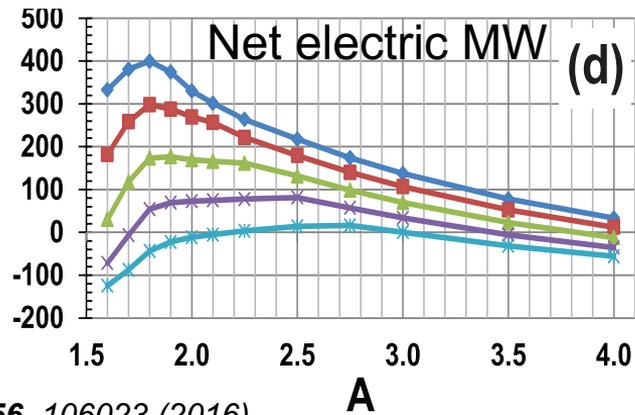
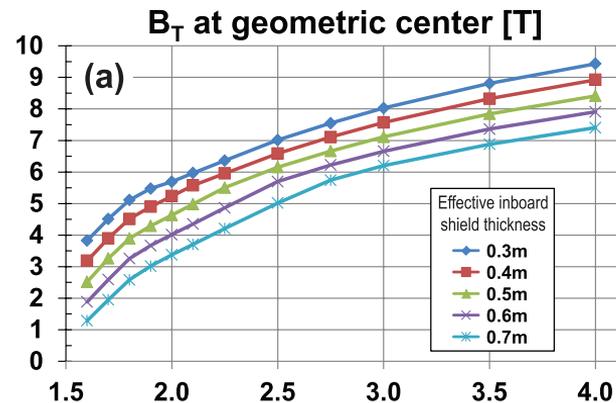
# Spherical tokamaks look more like a cored apple



MAST experiment  
in the U.K.

# Compact tokamak design studies show impact of aspect ratio on performance

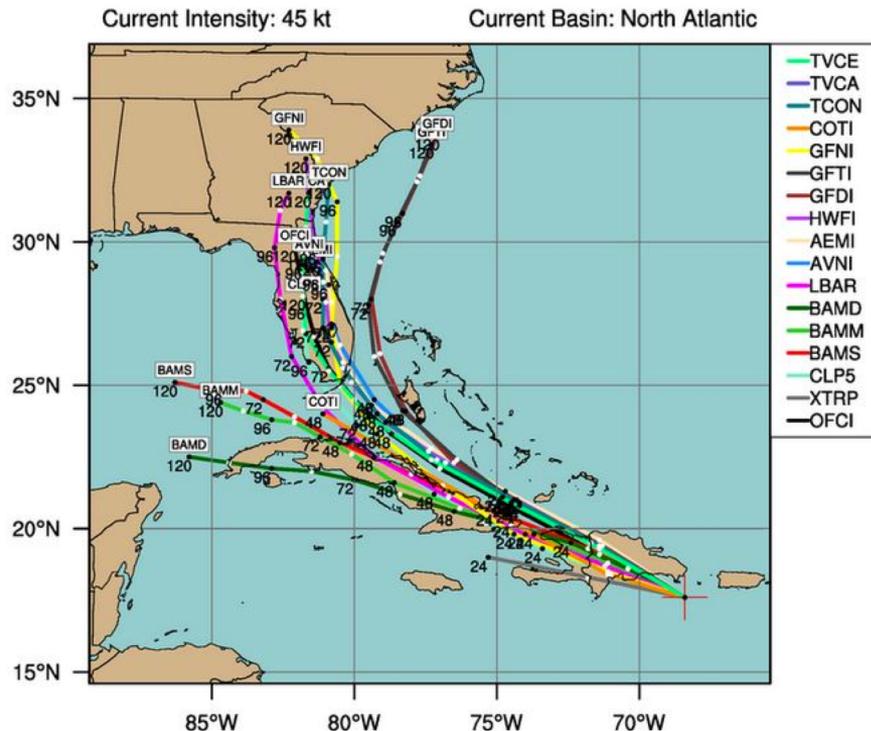
- Design study fixed size of cryostat and 50 MW of heating power
  - Assumes high-temperature superconducting magnets are available
- Optimization in design studies depends on validated models
  - Both in plasma physics and engineering



Cryostat volume ~ 1/3 of ITER

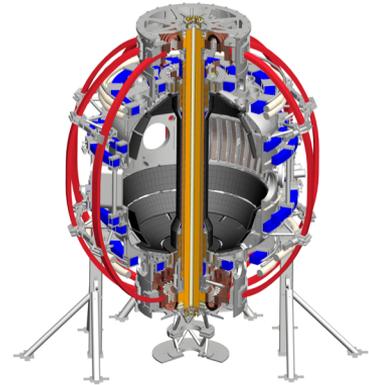
# Confident projections require validated models

- Will probably need to be confident that a fusion reactor concept will work before it gets an investor
  - Like hurricanes, non-linear multi-scale plasma physics is complicated
- Build experiments to challenge and validate models
  - Present day experiments are "wind tunnels"
    - For example, only deuterium fuel is used
  - Models, design and analysis all aided by advances in computational power

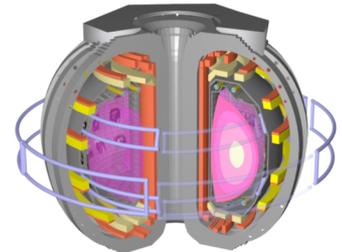


# Is there a “sweet spot” in the aspect ratio for compact tokamak reactors?

- Fusion power density:  $P_{\text{fusion}}/\text{volume} \propto \beta_{\text{T}}^2 B_{\text{T}}^4$ 
  - $\beta_{\text{T}}$  is limited by the pressure limits
  - $B_{\text{T}}$  set by magnet engineering and shielding constraints
- Spherical tokamaks (lower  $A$ ) have larger  $\beta_{\text{T}}$ , but lower  $B_{\text{T}}$
- Characteristics of turbulence, stability and current drive vary with  $\beta_{\text{T}}$  and aspect ratio
  - Two US tokamaks provide bookends in aspect ratio for developing and testing models



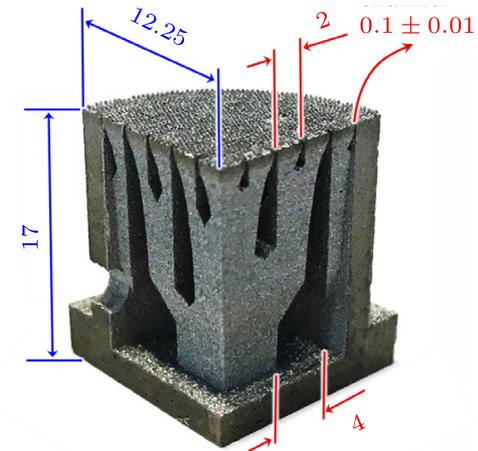
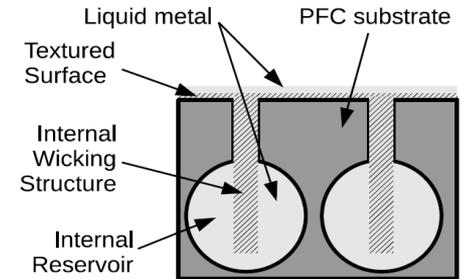
NSTX-U,  $A = 1.8$   
Princeton, NJ



DIII-D,  $A = 3$   
San Diego, CA

# Tokamaks are used as a test-bed for technology development needed for fusion reactors

- Fusion reactors require plasma facing surfaces that are resilient to the large neutron and energy flux
  - Challenge becomes more critical in a compact design
- Liquid metal walls are a solution with the ability to self-heal, replenish and dissipate energy (evaporation and flow)
- NSTX-U is preparing for large-scale test of liquid lithium PFCs in a magnetic confinement device
  - This is just one example of the fusion R&D being pursued on tokamak devices that benefits all MCF schemes





# In summary ...

- Tokamaks create a helical magnetic field by driving a toroidal current in the plasma
  - Demonstrated the highest  $p\tau$  (pressure x energy confinement time) of any magnetic confinement concept (to date)
  - Useful devices for producing high temperature plasmas for sec. to minutes
    - ITER will produce plasmas that last minutes
    - Next frontier is demonstrating longer pulse tokamaks at high  $p\tau$
- Two operating tokamaks in the US: DIII-D (San Diego) and NSTX-U (Princeton)
  - Experiments support preparations for ITER operation
  - Span aspect ratio to validate science and engineering models needed to optimize the design of a compact tokamak pilot plant
  - Serve as a test-bed for R&D innovations that reduce the cost of a reactor

# Welcome to the NSTX-U control room!

- 20 – 40 scientists and engineers at any given time
  - Experiment is locked up for the day
  - All aspects controlled and monitored remotely
- One plasma discharge about every 20 minutes (25 – 30 per day)
  - Copper magnets need to cool down
  - Countdown clock keeps the pace of the day
- Each discharge lasts a few seconds
  - Longest discharges limited by component heating
  - Each discharge generates GBs of data
- Operate for 15 – 20 weeks per year
  - Down time spent on maintenance, upgrades, planning and analysis

Chief Operating Engineer

Physics Operator

Session leader

